

A Bibliography of Publications by, and about, Magnus Rudolph Hestenes

Nelson H. F. Beebe
University of Utah
Department of Mathematics, 110 LCB
155 S 1400 E RM 233
Salt Lake City, UT 84112-0090
USA

Tel: +1 801 581 5254

E-mail: beebe@math.utah.edu, beebe@acm.org,
beebe@computer.org (Internet)
WWW URL: <https://www.math.utah.edu/~beebe/>

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Abstract

6 [Tab70].

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70th [Rus76].

Title word cross-reference

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13-15 [Cra87]. 1968 [ZNB69]. 1970 [Rei71a]. 1987 [Cra87].

2 [Tab70]. 23 [PT53]. 2nd [ZNB69].

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Hes61b, Hes64, Hes66a, Hes80a, Hes87,

Jer77, Ste73, Buk67, You68]. **Three**

[AMI⁺21, BSA18, DHG⁺17, DLLL19, FA21,

HKH⁺22, KBA23b, LLW22, Wan23, ZZ12].

Three-Term

[AMI⁺21, BSA18, DHG⁺17, DLLL19, FA21,

HKH⁺22, KBA23b, Wan23, ZZ12]. **Time**

[Hes50b]. **Top** [Ano22, DS00]. **Toronto**

[Jer77]. **Transformations** [Hes62c].

Transforms [CC97]. **Tribus** [Fri73].

Tucker [BGR05]. **Two**

[WSH⁺17, Cag80, Sny82]. **two-point**

[Sny82]. **two-sided** [Cag80]. **Type**

[AMI⁺21, DLL⁺17, HKH⁺22, Heg88b,

Heg88a, Sny82].

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[HAE21, DLL⁺17, NK21, RMMF10, Wan23].

understanding [CLS24]. **University**

[Rus76]. **use** [SW75]. **Using** [CMN18].

V [Dre65, Tab70]. **Value** [WZ14, Sny82].

Variable [Hes32b, Hes31, Hes32a, Hes33b].

Variational [Gui65b, Hes64, Hes65, Hes69c,

Hes54, Hes61b, Hes83, Hes87]. **Variations**

[BH35a, BH35c, BH35d, Buk67, Hes33e,

HB33, Hes34d, Hes49, Hes50a, Hes50b,

Hes56b, Hes66b, Hes80b, Hes13, Rus76, You68, BH35b, BH32, BH33a, BH33b, Bol01, Hes33a, Hes33d, Hes33c, Hes34b, Hes34c, Hes34e, Hes36c, Hes37, Hes38, Hes39, HR39, HM40, Hes41b, Hes42, Hes46a, Hes46b, Hes46c, Hes48, Hes51a, Hes66a]. **vectors** [HK51b]. **versions** [Zha09].

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xiii [Jer77]. xxii [Dea64].

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